## CGO - Costly Global Optimization



The **TOMLAB /CGO** toolbox efficiently solves global non-convex (integer) problems where the function f(x) is very costly to compute.

The toolbox consists of three general solvers:

- rbfSolve using a Radial Basis Interpolation (RBF) algorithm.
- ego using the Efficient Global Optimization (EGO) algorithm.
- arbfMIP new Adaptive Radial Basis Interpolation (ARBF) algorithm.



Response surface methods were discussed in a paper by Donald R. Jones:

A Taxonomy of Global optimization Methods Based on Response Surfaces Journal of Global Optimization 21 (4), 345:383, 2001.

Jones draws the conclusion that methods based on EGO and RBF algorithms are the most promising. The TOMLAB /CGO toolbox is based on these promising methods, and has been continuously further developed along with the state-of-the-art research in the field.

One previous example that motivated the research was industrial design of trains, where one f(x) value took 30 minutes to compute. The function value was the result of a simulation of 30 second train ride. This problem is discussed in the paper:

Mattias Björkman, Kenneth Holmström: *Global Optimization of Costly Nonconvex Functions Using Radial Basis Functions*, **Optimization and Engineering 1,** 373-397, 2000.

The train design included costly nonlinear constraints. They were assigned a weight and added to the objective function. This approach showed to be very successful. The choice of weights were not crucial.

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## Main Features

- rbfSolve, EGO and arbfMIP have shown good results in practice on industrial and financial problems.
- > All solvers are completely integrated in the TOMLAB Optimization Environment, and easy to combine with other solvers in TOMLAB.
- It is easy to use warm starts, and combine the EGO and (A)RBF solvers. The EGO solver sometimes have problem with ill-conditioning of the inverse of the correlation matrix when the number of sampled points grows. rbfSolve have showed to work without problems on up to 1000 points.



- > The initial set of points is important. The TOMLAB /CGO solvers have several ways to generate initial points. The user may also specify any number of initial points to include.
- > The TOMLAB /CGO solvers have several algorithmic options that may be tuned for the particular class of user problem.
- > It is recommended to combine this toolbox with TOMLAB /NPSOL or TOMLAB /SOL, using NPSOL as fast and robust local solver on the response surface.
- > Read more about the <u>rbfSolve</u> solver.
- Read more about the <u>ego</u> solver.
- > Read more about the <u>arbfMIP</u> solver.